




Gas Laws


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LPT




Rigid and Flexible Gas Containers



Walls: rigid
Volume: constant
Rupture when internal pressure exceeds container strength
Example: compressed gas cylinder




Walls: flexible
Volume: constant if internal & surroundings pressures equal
Volume: changes if internal & surroundings pressures unequal
Rupture when internal pressure exceeds container strength
Examples: balloon, internal air spaces (lungs, ears, sinus, gut)






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Joseph Louis Guy-Lussac
French chemist
Student of Jacques Charles
Studied Gases In Chemical Reactions



Pressure - Temperature relationship (1809)
Maybe called Charles's Law or Charles's Law #2
Sometimes called Amonton's Law
(Proposed relationship, but lacked technology to prove)

But,
Guy-Lussac was first to experimentally document P-T relation

His observations - primary source of absolute temperature scale



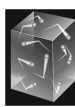
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Guy-Lussac's Law

Heat energy increases molecular motion.
Volume of cylinder cannot increase, the pressure increases

At constant *volume*, in a RIGID container:
pressure is directly proportional to the absolute temperature

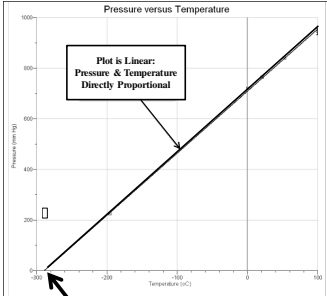



$$\frac{P_1}{T_1} = \frac{P_2}{T_2}$$



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Guy-Lussac's Law





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A sample of oxygen has a pressure of 1420. mm Hg at a temperature of 75 °C.
What is the pressure of this gas sample if temperature is lowered to 19° C?


| | Pressure (torr)* | Volume | Temperature (°C) | → | Temperature (K) |
|---------|------------------|----------|------------------|-------|-----------------|
| Initial | 1420 | constant | 75 | + 273 | 348 |
| Final | ? | constant | 19 | + 273 | 292 |

Volume constant, use Guy-Lussac's Law

$$\frac{P_1}{T_1} = \frac{P_2}{T_2}$$

$$\frac{1420 \text{ torr}}{348 \text{ K}} = \frac{P_2}{292 \text{ K}} \longrightarrow \frac{(1420 \text{ torr})(292 \text{ K})}{348 \text{ K}} = P_2$$

$P_2 = 1191.49 \text{ torr} \rightarrow 1190 \text{ torr} \rightarrow 1190 \text{ mm Hg}$



* 1 mm Hg = 1 torr

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Calculate the pressure a gas will exert at 65 °C if the gas has a pressure of 830. torr at 52 °C.

| | Pressure (torr) | Volume | Temperature (°C) | → | Temperature (K) |
|---------|-----------------|----------|------------------|-------|-----------------|
| Initial | 830 | constant | 52 | + 273 | 325 |
| Final | ? | constant | 65 | + 273 | 338 |

Volume constant, use Guy-Lussac's Law

$$\frac{P_1}{T_1} = \frac{P_2}{T_2}$$

$$\frac{830 \text{ torr}}{325 \text{ K}} = \frac{P_2}{338 \text{ K}} \longrightarrow \frac{(830 \text{ torr})(338 \text{ K})}{325 \text{ K}} = P_2$$

$$P_2 = 863.2 \text{ torr} \rightarrow 863 \text{ torr}$$



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A sample of nitrogen has a pressure of 1420. torr at a temperature of 75 °C. What is the °C temperature of this gas if the pressure is lowered to 258 torr?

| | Pressure (torr) | Volume | Temperature (°C) | → | Temperature (K) |
|---------|-----------------|----------|------------------|-------|-----------------|
| Initial | 1420 | constant | 75 | + 273 | 348 |
| Final | 258 | constant | ? | + 273 | ? |

Volume constant, use Guy-Lussac's Law

$$\frac{P_1}{T_1} = \frac{P_2}{T_2}$$

$$\frac{1420 \text{ torr}}{348 \text{ K}} = \frac{258 \text{ torr}}{T_2} \longrightarrow \frac{(258 \text{ torr})(348 \text{ K})}{(1420 \text{ torr})} = T_2$$

$$T_2 = 63.2262 \text{ K} \rightarrow T_2 = 63.2 \text{ K}$$

$$T_2 = 63.2 \text{ K} - 273 = -210 \text{ °C}$$



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Jacques Charles

French chemist
Scientific Advisor to
Montgolfier brothers



Volume - Temperature Relationship (1787)

1783 – First hot air balloon

Sack cloth and paper with 1800 buttons

Redesigned the way hot-air balloons were built:

Silk instead of paper construction

Hydrogen instead of hot air

Valve line

Wicker basket passenger compartment



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Charles' Law



Heat energy increases molecular motion.

Volume of flexible container increases

At constant *pressure*, in a FLEXIBLE container
volume is directly proportional to the absolute temperature

$$\frac{V_1}{T_1} = \frac{V_2}{T_2}$$



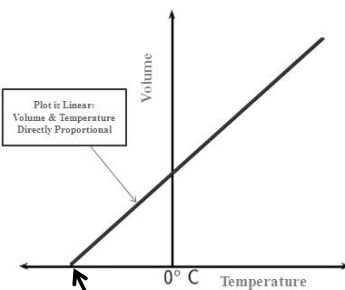
If $T = \text{negative}$, volume = negative (not realistic)

Need temperature to be positive

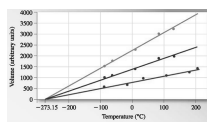
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Charles' Law



Absolute Zero (-273.16 °C)



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A sample of oxygen occupies a volume of 1240 mL at temperature of 45° C.
What is the volume of this gas sample if the temperature is raised to 85° C?

| | Pressure | Volume (mL) | Temperature (°C) | → | Temperature (K) |
|---------|----------|-------------|------------------|-------|-----------------|
| Initial | constant | 1240 | 45 | + 273 | 318 |
| Final | constant | ? | 85 | + 273 | 358 |

Pressure constant, use Charles' Law

$$\frac{V_1}{T_1} = \frac{V_2}{T_2}$$

$$\frac{1240 \text{ mL}}{318 \text{ K}} = \frac{V_2}{358 \text{ K}} \longrightarrow \frac{(1240 \text{ mL})(358 \text{ K})}{318 \text{ K}} = V_2$$

$$V_2 = 1395.97 \text{ mL} \rightarrow 1400 \text{ mL} \quad (1.40 \times 10^3 \text{ mL})$$



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Calculate the volume a gas will occupy at 15 °C if the gas has a volume of 830. mL at 42 °C.

| | Pressure | Volume (mL) | Temperature (°C) | → | Temperature (K) |
|---------|----------|-------------|------------------|-------|-----------------|
| Initial | constant | 830 | 42 | + 273 | 315 |
| Final | constant | ? | 15 | + 273 | 288 |

Pressure constant, use Charles' Law

$$\frac{V_1}{T_1} = \frac{V_2}{T_2}$$

$$\frac{830 \text{ mL}}{315 \text{ K}} = \frac{V_2}{288 \text{ K}} \longrightarrow \frac{(830 \text{ mL})(288 \text{ K})}{315 \text{ K}} = V_2$$

$$V_2 = 758.857 \text{ mL} \rightarrow 759 \text{ mL}$$



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Calculate the final temperature in °C of a gas initially at 39 °C whose volume changes from 348 ml to 657 mL. The pressure remains constant.

| | Pressure | Volume (mL) | Temperature (°C) | → | Temperature (K) |
|---------|----------|-------------|------------------|-------|-----------------|
| Initial | constant | 348 | 39 | + 273 | 312 |
| Final | constant | 657 | ? | + 273 | ? |

Pressure constant, use Charles' Law

$$\frac{V_1}{T_1} = \frac{V_2}{T_2}$$

$$\frac{348 \text{ mL}}{312 \text{ K}} = \frac{657 \text{ mL}}{T_2} \longrightarrow \frac{(657 \text{ mL})(312 \text{ K})}{(348 \text{ mL})} = T_2$$

$$T_2 = 589.038 \rightarrow 589 \text{ K}$$

$$T_2 = 589 \text{ K} - 273 = 316 \text{ °C}$$

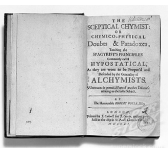


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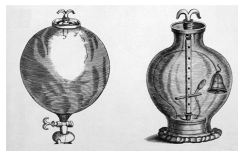
Robert Boyle
Irish Alchemist
Father of modern chemistry
Founder of Royal Society



Pressure - Volume relationship (1660)

New Experiments: Psico-Mechanical Touching the spring of air and their effects (1660)

The Sceptical Chymist (Air, Earth, Fire, & Water not elements) (1661)



In an evacuated chamber
Observed bubble in snake's eye
Reduced Pressure Changes Physiology
Bell produced no sound
Air needed to carry sound

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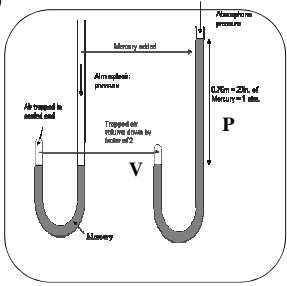

Boyles's Law Apparatus

Measure height mercury (P)
Measure Volume (V)

$P_1 V_1 = k$
 $P_2 V_2 = k$
 $P_3 V_3 = k$

Set Equalities

$P_1 V_1 = k = P_2 V_2$
 $P_1 V_1 = P_2 V_2$

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Boyles's Law

At constant *temperature*,
the volume of a flexible container
depends upon the surrounding pressure

At constant *temperature*, in a FLEXIBLE container
volume is indirectly proportional to the absolute pressure


$P_1 V_1 = P_2 V_2$

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Boyles's Law




Hyperbolic Curve:
Pressure & Volume
Inversely Proportional

Greatest volume change:
pressure near zero

Means greatest risk to tissue:
shallow water

Explains:

- Ear Discomfort while ascending / descending
- Grandpa's knee forecasting weather
- Changes in all gas volumes with altitude / depth
- Changes in pressure with altitude / depth



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At 723 mm Hg a gas has a volume of 294 mL. What is the new volume of this gas if the pressure is changed to 585 mm Hg?

| | Pressure (mm Hg) | Volume (mL) | Temperature (°C) | Temperature (K) |
|---------|---------------------|----------------|---------------------|--------------------|
| Initial | 723 | 294 | constant | constant |
| Final | 585 | ? | constant | constant |

Temperature constant, use Boyle's Law

$$P_1 V_1 = P_2 V_2$$

$$(723 \text{ mm Hg}) (294 \text{ mL}) = (585 \text{ mm Hg}) V_2$$

$$\frac{(723 \text{ mm Hg}) (294 \text{ mL})}{(585 \text{ mm Hg})} = V_2$$

$$V_2 = 363.354 \text{ mL} \rightarrow 363 \text{ mL}$$



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At 723 torr a gas has a volume of 294 mL. What is the new pressure of this gas if the volume is changed to 1256 mL?

| | Pressure (torr) | Volume (mL) | Temperature (°C) | Temperature (K) |
|---------|--------------------|----------------|---------------------|--------------------|
| Initial | 723 | 294 | constant | constant |
| Final | ? | 1256 | constant | constant |

Temperature constant, use Boyle's Law

$$P_1 V_1 = P_2 V_2$$

$$(723 \text{ torr}) (294 \text{ mL}) = (1256 \text{ mL}) P_2$$

$$\frac{(723 \text{ torr}) (294 \text{ mL})}{(1256 \text{ mL})} = P_2$$

$$P_2 = 169.237 \rightarrow 169 \text{ torr}$$



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General Gas Law

$$\frac{P_1 V_1}{t_1} = \frac{P_2 V_2}{t_2}$$



Units need to be same on both sides of =
P & T must be in absolute measures
Class assumes given P is absolute



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General Gas Law

$$\frac{P_1 V_1}{T_1} = \frac{P_2 V_2}{T_2}$$



If P constant:

$$\frac{V_1}{T_1} = \frac{V_2}{T_2}$$

Charles



If V constant:

$$\frac{P_1}{T_1} = \frac{P_2}{T_2}$$

Guy-Lussac



If T constant:

$$P_1 V_1 = P_2 V_2$$

Boyle



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A sample of neon with a volume of 825 mL at a temperature of 37 °C and a pressure of 600. torr is heated to a temperature of 68 °C and a pressure of 940. mm Hg. What is the new volume of the gas?

| | Pressure (torr) | Volume (mL) | Temperature (°C) | → | Temperature (K) |
|---------|-----------------|-------------|------------------|-------|-----------------|
| Initial | 600 | 825 | 37 | + 273 | 310 |
| Final | 940 | ? | 68 | + 273 | 341 |

Pressure, Volume & Temperature change, use General Gas Law

$$\frac{P_1 V_1}{T_1} = \frac{P_2 V_2}{T_2}$$

$$\frac{(600 \text{ torr}) (825 \text{ mL})}{310 \text{ K}} = \frac{(940 \text{ torr}) V_2}{341 \text{ K}} \rightarrow \frac{(600 \text{ torr}) (825 \text{ mL}) (341 \text{ K})}{(310 \text{ K}) (940 \text{ torr})} = V_2$$

$$V_2 = 579.255 \text{ mL} \rightarrow 579 \text{ mL}$$



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A sample of argon with a volume of 4.37 L at a temperature of 58 °C and a pressure of 725 torr is cooled to a temperature of 22 °C and a pressure of 615 mm Hg. What is the new volume of the gas?

| | Pressure (torr) | Volume (L) | Temperature (°C) | → | Temperature (K) |
|---------|-----------------|------------|------------------|-------|-----------------|
| Initial | 725 | 4.37 | 58 | + 273 | 331 |
| Final | 615 | ? | 22 | + 273 | 295 |

Pressure, Volume & Temperature change, use General Gas Law

$$\frac{P_1 V_1}{T_1} = \frac{P_2 V_2}{T_2}$$

$$\frac{(725 \text{ torr}) (4.37 \text{ L})}{331 \text{ K}} = \frac{(615 \text{ torr}) V_2}{295 \text{ K}} \rightarrow \frac{(725 \text{ torr}) (4.37 \text{ L}) (295 \text{ K})}{(331 \text{ K}) (615 \text{ torr})} = V_2$$

$$V_2 = 4.59133 \text{ L} \rightarrow 4.59 \text{ L}$$



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A sample of nitrogen with a volume of 14.7 L at a temperature of 95 °C and a pressure of 485 torr is brought to STP. What is the new volume?

| | Pressure (torr) | Volume (L) | Temperature (°C) | → | Temperature (K) |
|---------|-----------------|------------|------------------|-------|-----------------|
| Initial | 485 | 14.7 | 95 | + 273 | 368 |
| Final | 760 | ? | 0 | + 273 | 273 |

Pressure, Volume & Temperature change, use General Gas Law

$$\frac{P_1 V_1}{T_1} = \frac{P_2 V_2}{T_2}$$

$$\frac{(485 \text{ torr}) (14.7 \text{ L})}{368 \text{ K}} = \frac{(760 \text{ torr}) V_2}{273 \text{ K}} \rightarrow \frac{(485 \text{ torr}) (14.7 \text{ L}) (273 \text{ K})}{(368 \text{ K}) (760 \text{ torr})} = V_2$$

$$V_2 = 6.95922 \text{ L} \rightarrow 6.96 \text{ L}$$



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A sample of neon at STP has a volume of 286 L. What is the pressure in atmospheres if the temperature is changed to 95 °C at a new volume of 26.5 L?

| | Pressure (ata)* | Volume (L) | Temperature (°C) | → | Temperature (K) |
|---------|-----------------|------------|------------------|-------|-----------------|
| Initial | 1.00 | 286 | 0 | + 273 | 273 |
| Final | ? | 26.5 | 95 | + 273 | 368 |

Pressure, Volume & Temperature change, use General Gas Law

$$\frac{P_1 V_1}{T_1} = \frac{P_2 V_2}{T_2}$$

$$\frac{(1.00 \text{ ata}) (286 \text{ L})}{273 \text{ K}} = \frac{P_2 (26.5 \text{ L})}{368 \text{ K}} \rightarrow \frac{(1.00 \text{ ata}) (286 \text{ L}) (368 \text{ K})}{(273 \text{ K}) (26.5 \text{ L})} = P_2$$

$$P_2 = 14.5481 \text{ ata} \rightarrow 14.5 \text{ ata}$$



* ata = atmospheres absolute

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A sample of xenon with a volume of 825 mL at a temperature of 37 °C and a pressure of 600. torr is changed to a pressure of 940. mm Hg at a volume of 628 mL. What is the temperature in °C of the gas?

| | Pressure (torr) | Volume (mL) | Temperature (°C) | → | Temperature (K) |
|---------|-----------------|-------------|------------------|-------|-----------------|
| Initial | 600 | 825 | 37 | + 273 | 310 |
| Final | 940 | 628 | ? | + 273 | ? |

Pressure, Volume & Temperature change, use General Gas Law

$$\frac{P_1 V_1}{T_1} = \frac{P_2 V_2}{T_2}$$

$$\frac{(600 \text{ torr}) (825 \text{ mL})}{310 \text{ K}} = \frac{(940 \text{ torr}) (628 \text{ mL})}{T_2} \rightarrow \frac{(940 \text{ torr}) (628 \text{ mL}) (310 \text{ K})}{(600 \text{ torr}) (825 \text{ mL})} = T_2$$


$$T_2 = 369.695 \text{ K} \rightarrow 370 \text{ K}$$

$$T_2 = 370 \text{ K} - 273 = 97 \text{ °C}$$




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Proportional Thinking



$$\frac{pv}{t} = k$$






$$\frac{p_1 v_1}{t_1} = k = \frac{p_2 v_2}{t_2}$$






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Proportional Thinking

$$\frac{pv}{t} = k$$








| | | |
|---|---|--|
| <p>If P constant:</p> $\frac{v}{t} = k$ <p>Charles' Law Direct Proportion</p>  | <p>If V constant:</p> $\frac{p}{t} = k$ <p>Guy-Lussac's Law Direct Proportion</p>  | <p>If T constant:</p> $pv = k$ <p>Boyle's Law Inverse Proportion</p>  |
|---|---|--|




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Proportional Thinking

$$\frac{pv}{t} = k$$

Variables change to keep k constant

| | | |
|---|---|--|
| <p>If P constant:</p> $\uparrow \frac{v}{t} = k$ <p>\uparrow</p> <p>v and t change (increase or decrease) in same direction</p>  | <p>If V constant:</p> $\uparrow \frac{p}{t} = k$ <p>\uparrow</p> <p>p and t change (increase or decrease) in same direction</p>  | <p>If T constant:</p> $pv = k$ <p>$\uparrow \downarrow$</p> <p>p and v change (increase or decrease) in opposite direction</p>  |
|---|---|--|







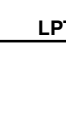

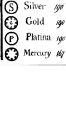


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Proportional Thinking: Word problems

At constant volume, if temperature decreases, pressure

At constant pressure, if temperature increases, volume

At constant temperature, if pressure increases, volume

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Proportional Thinking: Word problems

At constant volume, if temperature decreases, pressure decreases






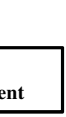
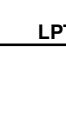

$\frac{P}{T} = k \rightarrow \frac{\downarrow P}{\downarrow T} = k$ P & T Move same direction

At constant pressure, if temperature increases, volume increases

$\frac{V}{T} = k \rightarrow \frac{\uparrow V}{\uparrow T} = k$ V & T Move same direction

At constant temperature, if pressure increases, volume decreases

$PV = k \rightarrow \frac{\uparrow P}{\downarrow V} = k$ P & V Move opposite direction

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John Dalton

School teacher with contributions to:
Atomic Theory
Understanding Color Blindness
Studies on Gas Behavior

Dalton's Law of Partial Pressure (1803)

$$P_{\text{total}} = P_1 + P_2 + P_3 + \dots P_n$$

For a mixture of ideal gases,
total pressure = sum of the partial pressures of gases present

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Dalton's Law: Partial Pressures

Dalton's law: In a mixture of gases, the total pressure is the sum of the partial pressures of the individual components

$$P = P_1 + P_2 + P_3 + \dots + P_n$$

The partial pressure of a gas is the product of the fraction of that gas times the total pressure

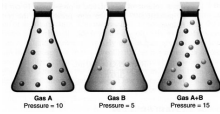
$$P_g = F_g \times P_{\text{total}}$$

Where

P_g = partial pressure of the component gas

F_g = fraction of the component gas in the mixture

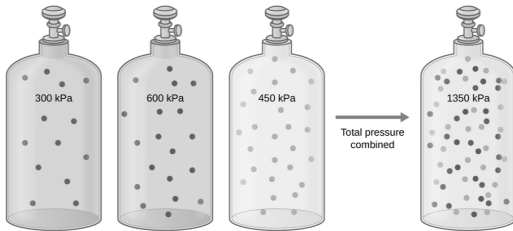
P_{total} = the total pressure of the gas mixture



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Dalton's Law: Partial Pressures



Total pressure is always the sum of component gas pressures

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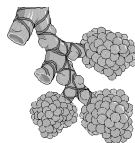
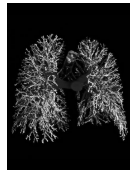
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Dalton's Law: Partial Pressures

Pressure in alveolar spaces immediately equilibrates with blood



| | Inspired air | Alveolar air |
|------------------|--------------|--------------|
| H ₂ O | Variable | 47 mmHg |
| CO ₂ | 000.3 mmHg | 40 mmHg |
| O ₂ | 159 mmHg | 105 mmHg |
| N ₂ | 601 mmHg | 568 mmHg |
| Total pressure | 760 mmHg | 760 mmHg |



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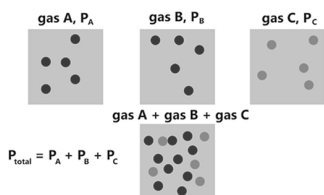
A mixture of gases at 760 torr contains 55.0 % N₂, 25.0 % O₂, and 20.0 % CO₂ by volume. What is the partial pressure of each gas?

$$\text{N}_2: 55.0/100 \times 760 \text{ torr} = 418 \text{ torr}$$

$$\text{O}_2: 25.0/100 \times 760 \text{ torr} = 190 \text{ torr}$$

$$\text{CO}_2: 20.0/100 \times 760 \text{ torr} = 152 \text{ torr}$$

$$\text{Total (check)} = 760 \text{ torr}$$



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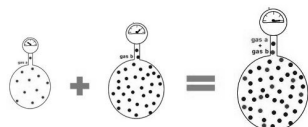
A 200 mL flask contains O₂ at 220 torr and a 300 mL flask contains N₂ at 100 torr. The flasks are connected and the gases are allowed to completely fill the system. There is no temperature change. What is the partial pressure of each gas and the total pressure?

The final volume is 200 mL + 300 mL = 500 mL

$$\text{O}_2: 220 \text{ torr} (200 / 500) = 88 \text{ torr}$$

$$\text{N}_2: 100 \text{ torr} (300 / 500) = 60 \text{ torr}$$

$$\text{Total: } 60 \text{ torr} + 88 \text{ torr} = 148 \text{ torr}$$



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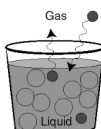
William Henry

British chemist

Solubility of gases

Composition of HCl and NH₃

Disinfecting powers of heat



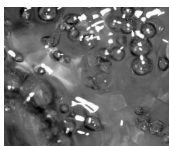
Gas in liquid solubility: Henry's Law (1803)

Determined solubility of gases in liquids a function of:

Partial pressure of the gas

Temperature of the system

Characteristics of the liquid



Very important when environmental pressure changes (alters gasses dissolved in the body)

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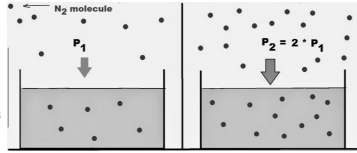
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Henry's Law

The amount of any given gas that will dissolve in a liquid at a given temperature is a function of the partial pressure of the gas that is in contact with the liquid and the solubility coefficient of the gas in the particular liquid

$$S_g = K_H \times P_g$$

S_g solubility of the gas
 K_H liquid solubility constant
 P_g Partial pressure of the gas



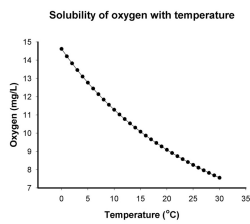
Increase in pressure → increase in solubility
 Decrease in pressure → decrease in solubility

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Henry's Law

Gas solubility changes with temperature



Colder water (Great Lakes): Divers carry additional gas loads

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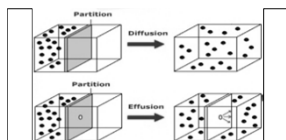
Graham's Law



The speed of gas diffusion (gas mixing due to kinetic energy) or effusion (gas moving through a tiny opening) is inversely proportional to the square root of their molar masses.

This is commonly written for effusion:

$$\frac{\text{Rate}_1}{\text{Rate}_2} = \sqrt{\frac{M_2}{M_1}}$$

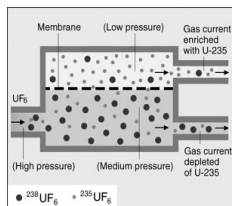
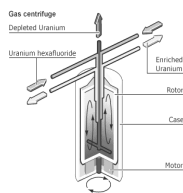


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Graham's Law

Useful for:
separation of gases of different densities
separation of isotopes
prime means for producing nuclear material
determining molar mass of unknown material



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Compare the relative rates of effusion of H_2 and CO through a fine pinhole.

Molar masses:

$CO = 28.0$
 $H_2 = 2.00$

$$\frac{\text{Rate } H_2}{\text{Rate } CO} = \sqrt{\frac{28.0}{2.00}} = 3.74$$

Compare the relative rates of effusion of H_2 and O_2 through a fine pinhole.

Molar masses:

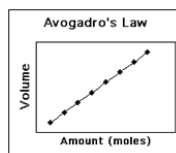
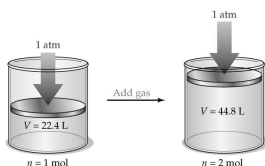
$O_2 = 32.0$
 $H_2 = 2.0$

$$\frac{\text{Rate } H_2}{\text{Rate } O_2} = \sqrt{\frac{32.0}{2.0}} = 4.0$$



Avogadro's Law (1811)

More Moles (Molecules) means more molecular collisions




Plot is Linear:
Volume & # moles
Directly Proportional

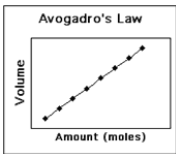



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Avagadro's Law

At constant *temperature and pressure*,
volume is directly proportional to the number of moles present



$$\frac{V_1}{n_1} = \frac{V_2}{n_2}$$

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1.00 mole of gas occupies 1.45L. If the quantity of gas is increased to 2.50 moles, what is the new volume of gas?


| | Pressure (torr) | Volume (L) | # moles |
|---------|-----------------|------------|---------|
| Initial | constant | 1.45 | 1.00 |
| Final | constant | ? | 2.50 |

Pressure constant, use Avagadro's Law


$$\frac{V_1}{n_1} = \frac{V_2}{n_2}$$

$$\frac{1.45 \text{ L}}{1.00 \text{ m}} = \frac{V_2}{2.50 \text{ m}} \longrightarrow V_2 = \frac{(1.45 \text{ L})(2.50 \text{ m})}{1.00 \text{ m}}$$


$$V_2 = 3.625 \text{ L} \longrightarrow 3.63 \text{ L}$$


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Ideal Gas Law



$$PV = kT$$

Pressure

Number of moles

Temperature

$$R = \frac{PV}{nT}$$

$$PV = nRT$$

Volume

Gas constant

R makes "numbers work"

For:
P in atm; V in L; T in K
R = universal gas constant: 0.08206 L · atm / K · mol

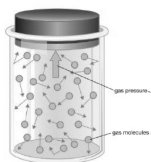
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Ideal Gas Law

$$PV = nRT$$

Based on kinetic theory of gases

Primary use is single point determination



Assumes:

Volume of individual gas molecules is negligible

There is no attraction between individual molecules

Strongest correlation between calculated and measured:

Low pressure

High temperature

Monatomic gases

Ideal gas law assumes vast distances between gas molecules

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Calculate the pressure of a 2.50 mole sample of a gas in a 5.50 L container at 27 °C.

Only one condition given → use Ideal Gas Law:

$$PV = nRT$$

$$P (5.50 \text{ L}) = (2.50 \text{ mole}) (0.08206 \text{ L-atm/K-mol}) (27 + 273 \text{ K})$$

$$P = \frac{(2.50 \text{ mole}) (0.08206 \text{ L-atm/K-mol}) (300 \text{ K})}{(5.50 \text{ L})}$$

$$P = 11.19 \text{ atm} \rightarrow 11.2 \text{ atm}$$

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How many moles of a gas occupy 2.67 L at STP?

Only one condition given → use Ideal Gas Law:

STP: Standard Temperature & Pressure → 1 atm and 273 K

$$PV = nRT$$

$$(1.00 \text{ atm}) (2.67 \text{ L}) = n (0.08206 \text{ L-atm/K-mol}) (273 \text{ K})$$

$$n = \frac{(1.00 \text{ atm}) (2.67 \text{ L})}{(0.08206 \text{ L-atm/K-mol}) (273 \text{ K})}$$

$$n = 0.119184 \rightarrow 0.119 \text{ mole}$$

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Real (Non-Ideal) Gases

Ideal gases (because of decreased distance between molecules) often will differ in behavior from ideal gas equations. Modifications of ideal laws to account for molecular volumes and attractions are termed Real or non-ideal situations.

Van der Waals' Real Gas Equation

Modifies ideal gas law to account for molecular volume and attractions

New Volume term: $V-nb$ (n = moles; b = specific constant for each gas)

New Pressure term: $P + \frac{an^2}{V^2}$ (a = specific constant for each gas)

$$(P + \frac{an^2}{V^2})(V-nb) = nRT$$

Values of a and b available in gas tables

Complex calculations best done by calculator / computer

Solving Gas Law Problems: Merely a Matter of Paying Attention to Details!



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